
Code No. : 81-E

## CCE PF CCE PR

ఎిజ్టయ : గగణిత్ర

Subject : MATHEMATICS<br>(ఇంగ్లిజ్ భలషాంతర / English Version)<br>



General Instructions :
i) The Question-cum-Answer Booklet consists of objective and subjective types of questions having 50 questions.
ii) Space has been provided against each objective type question. You have to choose the correct choice and write the complete answer along with its letter in the space provided.
iii) For subjective type questions enough space for each question has been provided. You have to answer the questions in the space.
iv) Follow the instructions given against both the objective and subjective types of questions.
v) Candidates should not write the answer with pencil. Answers written in pencil will not be evaluated. (Except Graphs, Diagrams \& Maps )
vi) In case of Multiple Choice, Fill in the blanks and Matching questions, scratching / rewriting / marking is not permitted, thereby rendering to disqualification for evaluation.
vii) Candidates have extra 15 minutes for reading the question paper.
viii) Space for Rough Work has been printed and provided at the bottom of each page.
ix) Do not write anything in the space provided in the right side margin.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its letter in the space provided against each question.

1. If $T_{n}=n^{2}+3$ then the value of $T_{3}$ is
(A) 6
(B) 9
(C) 12
(D) 27 .
2. Arithmetic mean of 2 and 8 is
(A) 5
(B) 10
(C) 16
(D) $3 \cdot 2$.
3. If the probability of winning a game is $0 \cdot 3$, then what is the probability of losing it ?
(A) $0 \cdot 1$
(B) $0 \cdot 3$
(C) $0 \cdot 7$
(D) $1 \cdot 3$.
4. The degree of the polynomial $2 x^{2}-4 x^{3}+3 x+5$ is
(A) 0
(B) 1
(C) 2
(D) 3 .
5. The distance between the origin and the point $(4,-3)$ is
(A) 1 unit
(B) 5 units
(C) 7 units
(D) -12 units.
6. The slope of the straight line whose inclination is $60^{\circ}$ is
(A) 0
(B) $\frac{1}{\sqrt{3}}$
(C) $-\sqrt{3}$
(D) $\sqrt{3}$.
7. If $\sin \theta=\frac{3}{5}$, then the value of $\operatorname{cosec} \theta$ is
(A) $\frac{4}{5}$
(B) $\frac{5}{3}$
(C) $\frac{4}{3}$
(D) $\frac{5}{4}$.
8. If the standard deviation of a set of scores is $1 \cdot 2$ and their mean is 10 , then the coefficient of variation of the scores is
(A) 12
(B) $0 \cdot 12$
(C) 20
(D) 120 .
II. Answer the following :
9. If $U=\{1,2,3,4,5\}$ and $A=\{2,4,5\}$ then find $A^{\prime}$.
10. The H.C.F. of 12 and 18 is 6 . Find their L.C.M.
11. If $f(x)=2 x^{2}+3 x+2$ then find the value of $f(2)$.
12. Two circles of diameters 10 cm and 4 cm , touch each other externally. Find the distance between their centres.
13. State Pythagoras theorem.
14. Write the formula to find the total surface area of a cylinder.
III. 15. Calculate the maximum number of diagonals that can be drawn in an
15. Prove that $2+\sqrt{5}$ is an irrational number.
16. There are 500 wrist watches in a box. Out of these 50 wrist watches are found defective. One watch is drawn randomly from the box. Find the probability that wrist watch chosen is a defective watch.
17. Find the product of $\sqrt{3}$ and $\sqrt[3]{2}$.
18. Rationalise the denominator and simplify :

$$
\frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}
$$

20. Find out the quotient and the remainder when
$P(x)=x^{3}+4 x^{2}-5 x+6$ is divided by $g(x)=x+1$.
OR
Find the polynomial which is to be added to
$P(x)=x^{4}+2 x^{3}-2 x^{2}+x-1$ so that the resulting polynomial is exactly divisible by $x^{2}+2 x-3$.
21. In the following figure, $D E \| A B$. If $A D=7 \mathrm{~cm}, C D=5 \mathrm{~cm}$ and $B C=18 \mathrm{~cm}$, find $C E$.

22. Given $\sqrt{3} \tan \theta=1$ and $\theta$ is an acute angle. Find the value of $\sin 3 \theta$.
23. Find the coordinates of the mid-point of the line segment joining the points (2, 3 ) and (4, 7 ).
24. The radius of a cone is 7 cm and its slant height is 10 cm . Calculate the curved surface area of the cone.

## OR

Calculate the volume of a right circular cylinder whose radius is 7 cm and height is 10 cm .

## ( SPACE FOR ROUGH WORK )

25. Solve the quadratic equation $x^{2}-4 x+2=0$ by formula method. 2
26. Construct a tangent at any point $P$ on a circle of radius 3 cm . 2
27. Draw a plan using the information given below :
[Scale: $20 \mathrm{~m}=1 \mathrm{~cm}$ ]

|  | Metre To D |  |
| :---: | :---: | :---: |
|  | 160 |  |
| 40 to E | 120 | 60 to C |
|  | 80 |  |
|  | 40 | 40 to B |
|  | From A |  |

28. In a group of people, 12 people know music, 15 people know drawing and 7 people know both music and drawing. If people know either music or drawing then calculate the number of people in the group. 2
29. A solid hemisphere of wax of radius 12 cm is melted and made into a cylinder of its base radius 6 cm . Calculate the height of the cylinder.

2
30. Find the sum of first 20 terms of the series $4+7+10+$ $\qquad$
31. If $A=\{1,2,3,4\}, B=\{2,4,5\}$ and $C=\{1,3,5,6\}$ then find $A \cup(B \cap C)$.
32. $\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \ldots$ are in a harmonic progression. Find the tenth term of it using the formula.
33. Find the sum of the geometric series $1+\frac{1}{3}+\frac{1}{9}+\ldots$ up to $\infty$.
34. Simplify: $4 \sqrt{63}+5 \sqrt{7}-8 \sqrt{28}$.
35. In tossing a fair coin twice, find the probability of getting exactly one tail.
36. The number of students who are willing to join their favourite sports are shown in the table. Draw the pie chart to represent the given data :

| Name of the sport : | Football | Tennis | Hockey |
| :---: | :---: | :---: | :---: |
| Number of students : | 12 | 16 | 8 |

37. Form the quadratic equation whose roots are 5 and 7 .
38. If $k=\frac{1}{2} m v^{2}$ solve for " $v$ " and then find the value of $v$, if $k=100$ and $m=2$.
39. In the following figure, $\left\lfloor A B C=90^{\circ}, B D \perp A C, B D=8 \mathrm{~cm}\right.$, $A D=4 \mathrm{~cm}$. Find $C D$.

40. Find the total surface area of a sphere of radius 7 cm .
IV. 41. Prove that "If two circles touch each other externally then their centres and the point of contact are collinear".
41. Calculate the standard deviation for the following data :

| Class-intervals | frequency |
| :---: | :---: |
| $1-5$ | 4 |
| $6-10$ | 3 |
| $11-15$ | 2 |
| $16-20$ | 1 |
|  | $\mathrm{~N}=10$ |

43. Find how many 4-digit numbers can be formed using the digits $1,2,3,4,5,6$ without repetition of the digits. Find out how many of these are less than 5000 ?

OR
If $16 \cdot{ }^{n} P_{3}=13 \cdot{ }^{n+1} P_{3}$ then find $n$.
44. Prove that

$$
\frac{\sin \left(90^{\circ}-\theta\right)}{1+\sin \theta}+\frac{\cos \theta}{1-\cos \left(90^{\circ}-\theta\right)}=2 \sec \theta
$$

OR

If $A=60^{\circ}, B=30^{\circ}$ then verify that
$\cos (A+B)=\cos A \cdot \cos B-\sin A \cdot \sin B$.
( SPACE FOR ROUGH WORK )
45. Pupils of Xth Standard of a school had arranged for a function at a total cost of Rs. 1,000 which was to be shared equally among them. Since 10 of them failed to join the function each of them had to pay Rs. 5 more. Find the number of pupils in the class.

OR
If $m$ and $n$ are the roots of the equation $x^{2}-5 x+3=0$, find the values of
i) $(m+n)^{2}+(m-n)^{2}$
ii) $(m+n)^{3}+4 m n$.
46. In the right angled triangle $A B C,\left\lfloor A B C=90^{\circ} . A M\right.$ and $C N$ are the medians drawn from $A$ and $C$ respectively to $B C$ and $A B$. Show that $4\left(A M^{2}+C N^{2}\right)=5 A C^{2}$.


In the rhombus $A B C D$, show that $4 A B^{2}=A C^{2}+B D^{2}$.

( SPACE FOR ROUGH WORK )
V. 47. Prove that
"If two triangles are equiangular then their corresponding sides are in proportion."
48. Draw two direct common tangents to two circles of radii 4 cm and 2 cm whose centres are 8 cm apart. Measure the length of the tangents.
49. In an arithmetic progression, the sum of first term, third term and the fifth term is 39 and the sum of second term, fourth term and the sixth term is 51 . Find the tenth term of the sequence.

OR
In a geometric progression, the sum of the first 3 terms is 7 and the sum of the next 3 terms is 56 . Find the geometric progression.
50. Solve the equation graphically :

$$
x^{2}+x-2=0
$$

graph

